



# Creating virtually distortion free imagery

## Geometric calibration of the Leica RC30

Ruedi Wagner, Vice President Imaging  
Udo Tempelmann, Head System Engineering  
Leica Geosystems, Geospatial Solutions Division

12.2.2012

The power to see



- when it has to be right





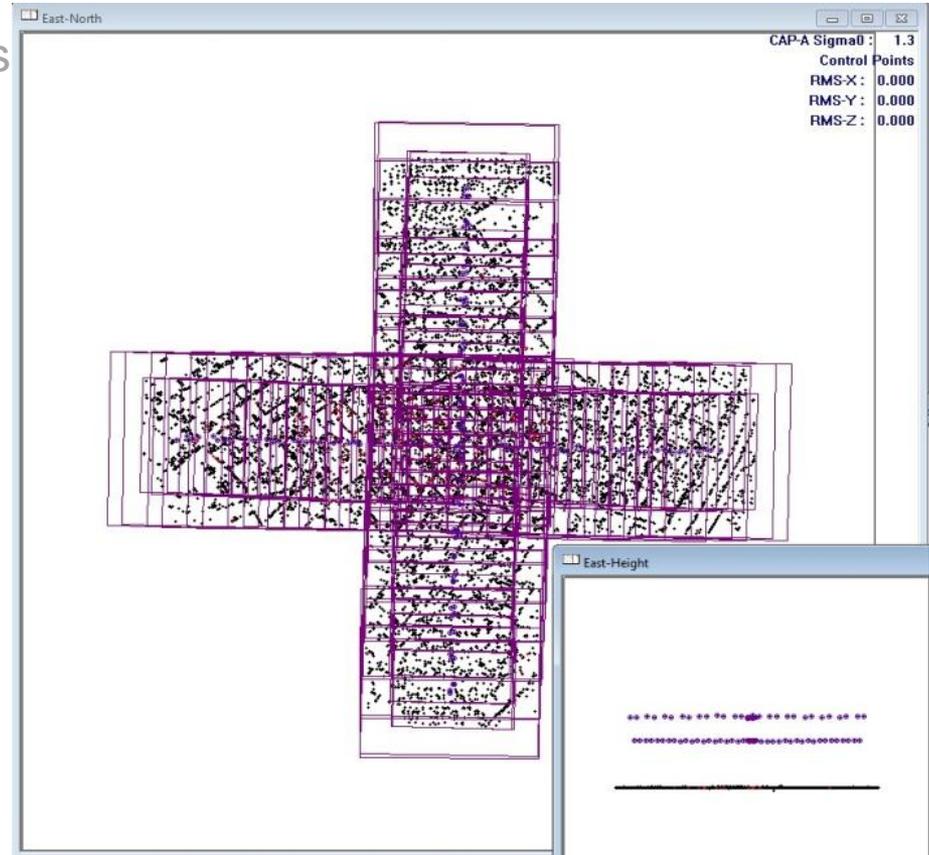
# Content

- RCD 30 sensor overview
- Photogrammetric flight calibration & grid based correction
- Goniometer approach, a small Leica history summary
- The RCD30 laboratory calibration



## Flight based calibration

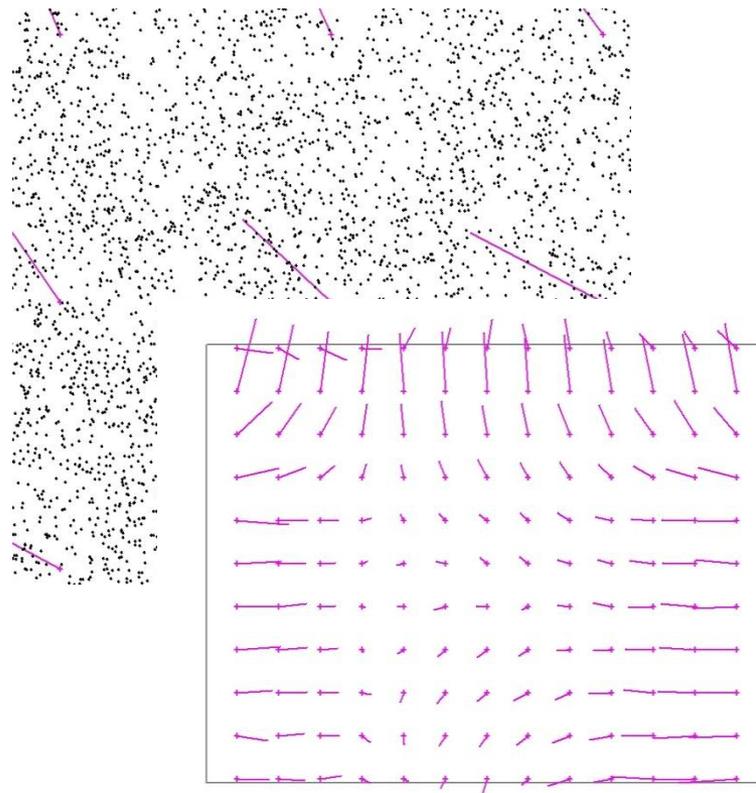
- Cross pattern at two different heights
- Symmetric, all line bi-directional
- Tie points with high number of rays
- GPS/IMU result from two heights allows calibration without ground control points
  
- Minimal correlation between camera parameters IMU misalignment and exterior orientation parameters



$k[2, 0] \mid 0_{\hat{1}}, 0_{\hat{2}} \rangle \cdot \langle 1_{\hat{1}}, 0_{\hat{2}} \mid + k[2, 1] \mid 0_{\hat{1}}, 1_{\hat{2}} \rangle \cdot \langle 1_{\hat{1}}, 0_{\hat{2}} \mid + k[0, 0] \mid 0_{\hat{1}}, 0_{\hat{2}} \rangle \cdot \langle 0_{\hat{1}}, 0_{\hat{2}} \mid + k[0, 1] \mid 0_{\hat{1}}, 1_{\hat{2}} \rangle \cdot \langle 0_{\hat{1}}, 0_{\hat{2}} \mid + k[4, 0] \mid 0_{\hat{1}}, 0_{\hat{2}} \rangle \cdot \langle 2_{\hat{1}}, 0_{\hat{2}} \mid + k[4, 1] \mid 0_{\hat{1}}, 1_{\hat{2}} \rangle \cdot \langle 2_{\hat{1}}, 0_{\hat{2}} \mid$   
 $k[2, 2] \mid 1_{\hat{1}}, 0_{\hat{2}} \rangle \cdot \langle 1_{\hat{1}}, 0_{\hat{2}} \mid + k[2, 3] \mid 1_{\hat{1}}, 1_{\hat{2}} \rangle \cdot \langle 1_{\hat{1}}, 0_{\hat{2}} \mid + k[0, 2] \mid 1_{\hat{1}}, 0_{\hat{2}} \rangle \cdot \langle 0_{\hat{1}}, 0_{\hat{2}} \mid + k[0, 3] \mid 1_{\hat{1}}, 1_{\hat{2}} \rangle \cdot \langle 0_{\hat{1}}, 0_{\hat{2}} \mid + k[4, 2] \mid 1_{\hat{1}}, 0_{\hat{2}} \rangle \cdot \langle 2_{\hat{1}}, 0_{\hat{2}} \mid + k[4, 3] \mid 1_{\hat{1}}, 1_{\hat{2}} \rangle \cdot \langle 2_{\hat{1}}, 0_{\hat{2}} \mid$   
 $k[2, 4] \mid 2_{\hat{1}}, 0_{\hat{2}} \rangle \cdot \langle 1_{\hat{1}}, 0_{\hat{2}} \mid + k[2, 5] \mid 2_{\hat{1}}, 1_{\hat{2}} \rangle \cdot \langle 1_{\hat{1}}, 0_{\hat{2}} \mid + k[0, 4] \mid 2_{\hat{1}}, 0_{\hat{2}} \rangle \cdot \langle 0_{\hat{1}}, 0_{\hat{2}} \mid + k[0, 5] \mid 2_{\hat{1}}, 1_{\hat{2}} \rangle \cdot \langle 0_{\hat{1}}, 0_{\hat{2}} \mid + k[4, 4] \mid 2_{\hat{1}}, 0_{\hat{2}} \rangle \cdot \langle 2_{\hat{1}}, 0_{\hat{2}} \mid + k[4, 5] \mid 2_{\hat{1}}, 1_{\hat{2}} \rangle \cdot \langle 2_{\hat{1}}, 0_{\hat{2}} \mid$   
 $k[3, 0] \mid 0_{\hat{1}}, 0_{\hat{2}} \rangle \cdot \langle 1_{\hat{1}}, 1_{\hat{2}} \mid + k[3, 1] \mid 0_{\hat{1}}, 1_{\hat{2}} \rangle \cdot \langle 1_{\hat{1}}, 1_{\hat{2}} \mid + k[1, 0] \mid 0_{\hat{1}}, 0_{\hat{2}} \rangle \cdot \langle 0_{\hat{1}}, 1_{\hat{2}} \mid + k[1, 1] \mid 0_{\hat{1}}, 1_{\hat{2}} \rangle \cdot \langle 0_{\hat{1}}, 1_{\hat{2}} \mid + k[5, 0] \mid 0_{\hat{1}}, 0_{\hat{2}} \rangle \cdot \langle 2_{\hat{1}}, 1_{\hat{2}} \mid + k[5, 1] \mid 0_{\hat{1}}, 1_{\hat{2}} \rangle \cdot \langle 2_{\hat{1}}, 1_{\hat{2}} \mid$   
 $k[3, 2] \mid 1_{\hat{1}}, 0_{\hat{2}} \rangle \cdot \langle 1_{\hat{1}}, 1_{\hat{2}} \mid + k[3, 3] \mid 1_{\hat{1}}, 1_{\hat{2}} \rangle \cdot \langle 1_{\hat{1}}, 1_{\hat{2}} \mid + k[1, 2] \mid 1_{\hat{1}}, 0_{\hat{2}} \rangle \cdot \langle 0_{\hat{1}}, 1_{\hat{2}} \mid + k[1, 3] \mid 1_{\hat{1}}, 1_{\hat{2}} \rangle \cdot \langle 0_{\hat{1}}, 1_{\hat{2}} \mid + k[5, 2] \mid 1_{\hat{1}}, 0_{\hat{2}} \rangle \cdot \langle 2_{\hat{1}}, 1_{\hat{2}} \mid + k[5, 3] \mid 1_{\hat{1}}, 1_{\hat{2}} \rangle \cdot \langle 2_{\hat{1}}, 1_{\hat{2}} \mid$   
 $k[3, 4] \mid 2_{\hat{1}}, 0_{\hat{2}} \rangle \cdot \langle 1_{\hat{1}}, 1_{\hat{2}} \mid + k[3, 5] \mid 2_{\hat{1}}, 1_{\hat{2}} \rangle \cdot \langle 1_{\hat{1}}, 1_{\hat{2}} \mid + k[1, 4] \mid 2_{\hat{1}}, 0_{\hat{2}} \rangle \cdot \langle 0_{\hat{1}}, 1_{\hat{2}} \mid + k[1, 5] \mid 2_{\hat{1}}, 1_{\hat{2}} \rangle \cdot \langle 0_{\hat{1}}, 1_{\hat{2}} \mid + k[5, 4] \mid 2_{\hat{1}}, 0_{\hat{2}} \rangle \cdot \langle 2_{\hat{1}}, 1_{\hat{2}} \mid + k[5, 5] \mid 2_{\hat{1}}, 1_{\hat{2}} \rangle \cdot \langle 2_{\hat{1}}, 1_{\hat{2}} \mid$

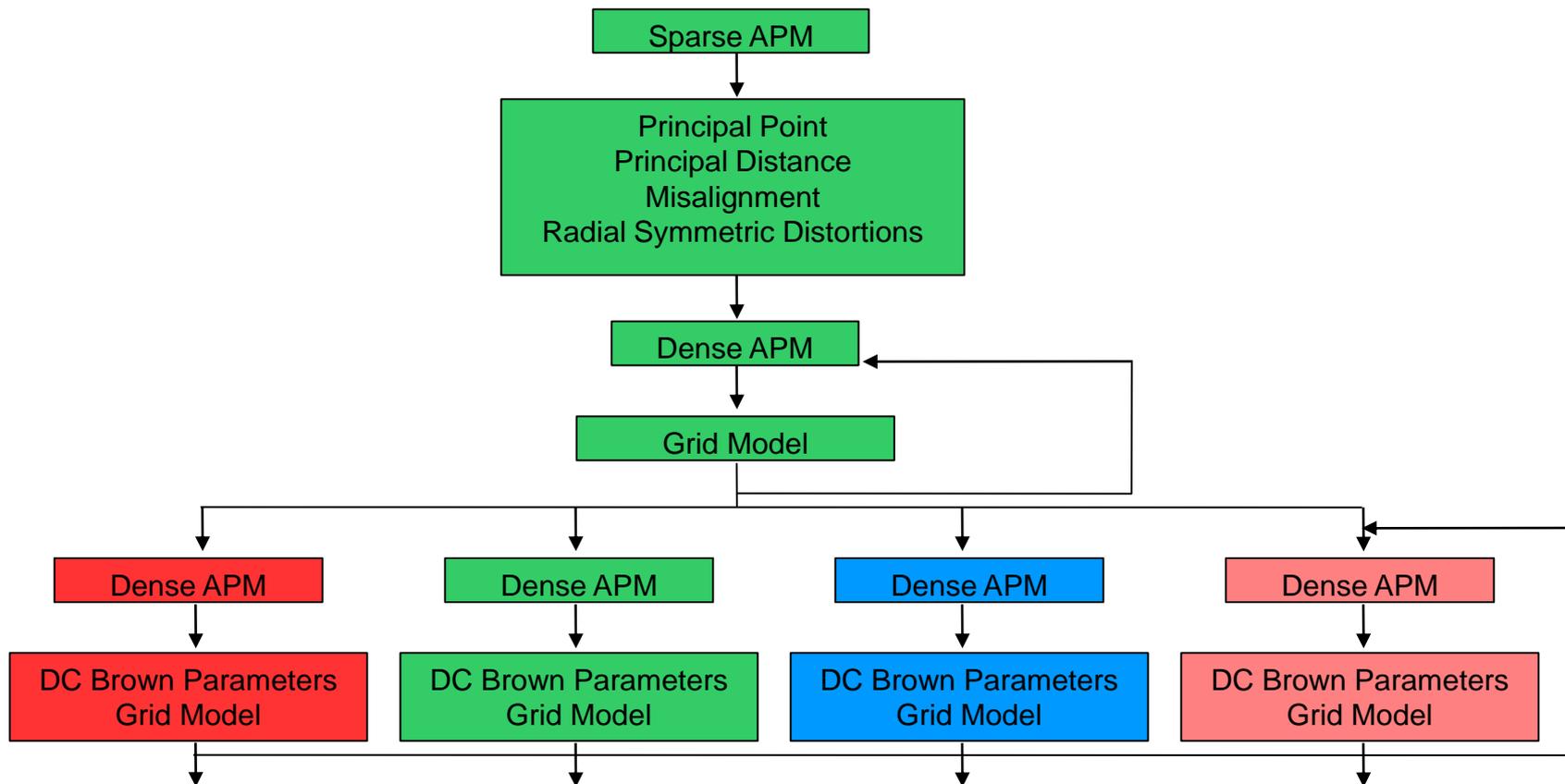
## Flight based calibration, the bundle adjustment

- DC Brown parameters used for the “classical” distortion model
- Grid estimation for local error
  - assumption error  $\approx 0$
  - integrated into the bundle
  - grid determined using the tie points of all images



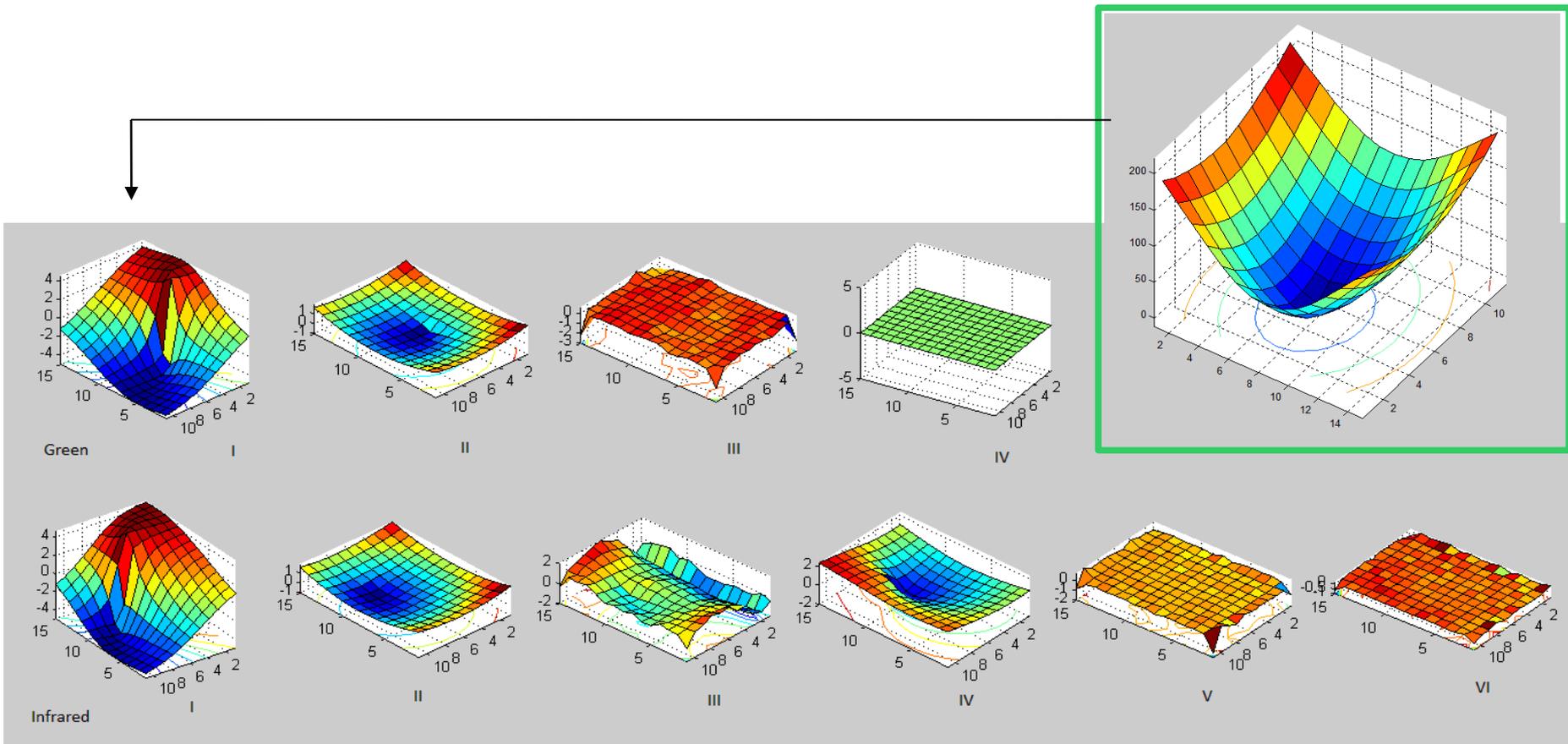
$k[2, 0] \mid 0_{i_1}, 0_{i_2} \cdot \langle 1_{i_1}, 0_{i_2} \mid +k[2, 1] \mid 0_{i_1}, 1_{i_2} \rangle \cdot \langle 1_{i_1}, 0_{i_2} \mid +k[0, 0] \mid 0_{i_1}, 0_{i_2} \rangle \cdot \langle 0_{i_1}, 0_{i_2} \mid +k[0, 1] \mid 0_{i_1}, 1_{i_2} \rangle \cdot \langle 0_{i_1}, 0_{i_2} \mid +k[4, 0] \mid 0_{i_1}, 0_{i_2} \rangle \cdot \langle 2_{i_1}, 0_{i_2} \mid +k[4, 1] \mid 0_{i_1}, 1_{i_2} \rangle \cdot \langle 2_{i_1}, 0_{i_2} \mid$   
 $k[2, 2] \mid 1_{i_1}, 0_{i_2} \rangle \cdot \langle 1_{i_1}, 0_{i_2} \mid +k[2, 3] \mid 1_{i_1}, 1_{i_2} \rangle \cdot \langle 1_{i_1}, 0_{i_2} \mid +k[0, 2] \mid 1_{i_1}, 0_{i_2} \rangle \cdot \langle 0_{i_1}, 0_{i_2} \mid +k[0, 3] \mid 1_{i_1}, 1_{i_2} \rangle \cdot \langle 0_{i_1}, 0_{i_2} \mid +k[4, 2] \mid 1_{i_1}, 0_{i_2} \rangle \cdot \langle 2_{i_1}, 0_{i_2} \mid +k[4, 3] \mid 1_{i_1}, 1_{i_2} \rangle \cdot \langle 2_{i_1}, 0_{i_2} \mid$   
 $k[2, 4] \mid 2_{i_1}, 0_{i_2} \rangle \cdot \langle 1_{i_1}, 0_{i_2} \mid +k[2, 5] \mid 2_{i_1}, 1_{i_2} \rangle \cdot \langle 1_{i_1}, 0_{i_2} \mid +k[0, 4] \mid 2_{i_1}, 0_{i_2} \rangle \cdot \langle 0_{i_1}, 0_{i_2} \mid +k[0, 5] \mid 2_{i_1}, 1_{i_2} \rangle \cdot \langle 0_{i_1}, 0_{i_2} \mid +k[4, 4] \mid 2_{i_1}, 0_{i_2} \rangle \cdot \langle 2_{i_1}, 0_{i_2} \mid +k[4, 5] \mid 2_{i_1}, 1_{i_2} \rangle \cdot \langle 2_{i_1}, 0_{i_2} \mid$   
 $k[3, 0] \mid 0_{i_1}, 0_{i_2} \rangle \cdot \langle 1_{i_1}, 1_{i_2} \mid +k[3, 1] \mid 0_{i_1}, 1_{i_2} \rangle \cdot \langle 1_{i_1}, 1_{i_2} \mid +k[1, 0] \mid 0_{i_1}, 0_{i_2} \rangle \cdot \langle 0_{i_1}, 1_{i_2} \mid +k[1, 1] \mid 0_{i_1}, 1_{i_2} \rangle \cdot \langle 0_{i_1}, 1_{i_2} \mid +k[5, 0] \mid 0_{i_1}, 0_{i_2} \rangle \cdot \langle 2_{i_1}, 1_{i_2} \mid +k[5, 1] \mid 0_{i_1}, 1_{i_2} \rangle \cdot \langle 2_{i_1}, 1_{i_2} \mid$   
 $k[3, 2] \mid 1_{i_1}, 0_{i_2} \rangle \cdot \langle 1_{i_1}, 1_{i_2} \mid +k[3, 3] \mid 1_{i_1}, 1_{i_2} \rangle \cdot \langle 1_{i_1}, 1_{i_2} \mid +k[1, 2] \mid 1_{i_1}, 0_{i_2} \rangle \cdot \langle 0_{i_1}, 1_{i_2} \mid +k[1, 3] \mid 1_{i_1}, 1_{i_2} \rangle \cdot \langle 0_{i_1}, 1_{i_2} \mid +k[5, 2] \mid 1_{i_1}, 0_{i_2} \rangle \cdot \langle 2_{i_1}, 1_{i_2} \mid +k[5, 3] \mid 1_{i_1}, 1_{i_2} \rangle \cdot \langle 2_{i_1}, 1_{i_2} \mid$   
 $k[3, 4] \mid 2_{i_1}, 0_{i_2} \rangle \cdot \langle 1_{i_1}, 1_{i_2} \mid +k[3, 5] \mid 2_{i_1}, 1_{i_2} \rangle \cdot \langle 1_{i_1}, 1_{i_2} \mid +k[1, 4] \mid 2_{i_1}, 0_{i_2} \rangle \cdot \langle 0_{i_1}, 1_{i_2} \mid +k[1, 5] \mid 2_{i_1}, 1_{i_2} \rangle \cdot \langle 0_{i_1}, 1_{i_2} \mid +k[5, 4] \mid 2_{i_1}, 0_{i_2} \rangle \cdot \langle 2_{i_1}, 1_{i_2} \mid +k[5, 5] \mid 2_{i_1}, 1_{i_2} \rangle \cdot \langle 2_{i_1}, 1_{i_2} \mid$

# An iterative process



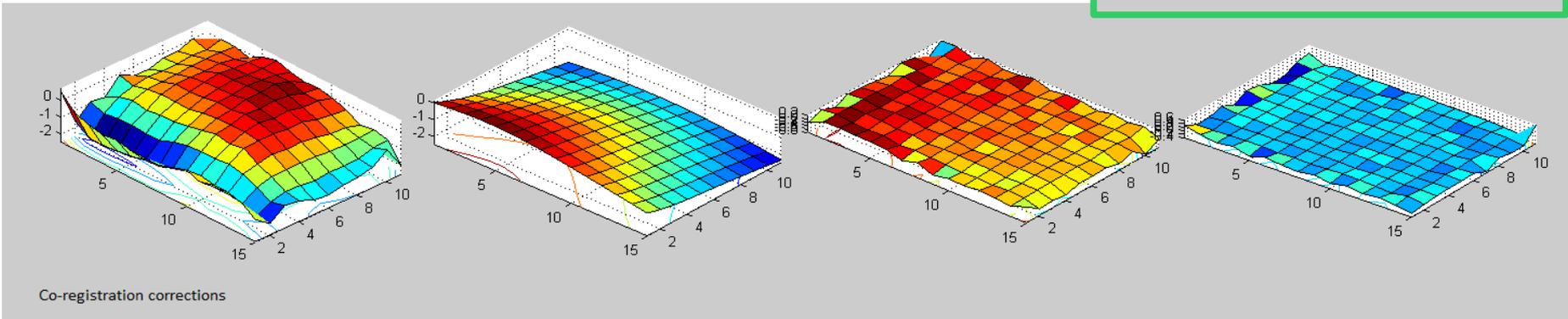
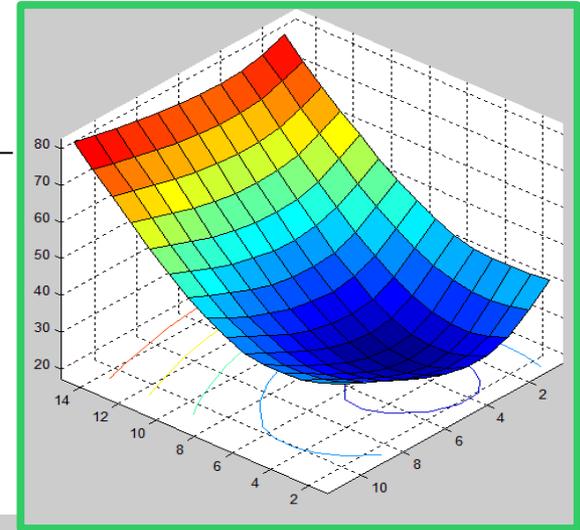
$k[2, 0] \mid 0_{\hat{i}}, 0_{\hat{z}} \rangle \cdot \langle 1_{\hat{i}}, 0_{\hat{z}} \mid + k[2, 1] \mid 0_{\hat{i}}, 1_{\hat{z}} \rangle \cdot \langle 1_{\hat{i}}, 0_{\hat{z}} \mid + k[0, 0] \mid 0_{\hat{i}}, 0_{\hat{z}} \rangle \cdot \langle 0_{\hat{i}}, 0_{\hat{z}} \mid + k[0, 1] \mid 0_{\hat{i}}, 1_{\hat{z}} \rangle \cdot \langle 0_{\hat{i}}, 0_{\hat{z}} \mid + k[4, 0] \mid 0_{\hat{i}}, 0_{\hat{z}} \rangle \cdot \langle 2_{\hat{i}}, 0_{\hat{z}} \mid + k[4, 1] \mid 0_{\hat{i}}, 1_{\hat{z}} \rangle \cdot \langle 2_{\hat{i}}, 0_{\hat{z}} \mid$   
 $k[2, 2] \mid 1_{\hat{i}}, 0_{\hat{z}} \rangle \cdot \langle 1_{\hat{i}}, 0_{\hat{z}} \mid + k[2, 3] \mid 1_{\hat{i}}, 1_{\hat{z}} \rangle \cdot \langle 1_{\hat{i}}, 0_{\hat{z}} \mid + k[0, 2] \mid 1_{\hat{i}}, 0_{\hat{z}} \rangle \cdot \langle 0_{\hat{i}}, 0_{\hat{z}} \mid + k[0, 3] \mid 1_{\hat{i}}, 1_{\hat{z}} \rangle \cdot \langle 0_{\hat{i}}, 0_{\hat{z}} \mid + k[4, 2] \mid 1_{\hat{i}}, 0_{\hat{z}} \rangle \cdot \langle 2_{\hat{i}}, 0_{\hat{z}} \mid + k[4, 3] \mid 1_{\hat{i}}, 1_{\hat{z}} \rangle \cdot \langle 2_{\hat{i}}, 0_{\hat{z}} \mid$   
 $k[2, 4] \mid 2_{\hat{i}}, 0_{\hat{z}} \rangle \cdot \langle 1_{\hat{i}}, 0_{\hat{z}} \mid + k[2, 5] \mid 2_{\hat{i}}, 1_{\hat{z}} \rangle \cdot \langle 1_{\hat{i}}, 0_{\hat{z}} \mid + k[0, 4] \mid 2_{\hat{i}}, 0_{\hat{z}} \rangle \cdot \langle 0_{\hat{i}}, 0_{\hat{z}} \mid + k[0, 5] \mid 2_{\hat{i}}, 1_{\hat{z}} \rangle \cdot \langle 0_{\hat{i}}, 0_{\hat{z}} \mid + k[4, 4] \mid 2_{\hat{i}}, 0_{\hat{z}} \rangle \cdot \langle 2_{\hat{i}}, 0_{\hat{z}} \mid + k[4, 5] \mid 2_{\hat{i}}, 1_{\hat{z}} \rangle \cdot \langle 2_{\hat{i}}, 0_{\hat{z}} \mid$   
 $k[3, 0] \mid 0_{\hat{i}}, 0_{\hat{z}} \rangle \cdot \langle 1_{\hat{i}}, 1_{\hat{z}} \mid + k[3, 1] \mid 0_{\hat{i}}, 1_{\hat{z}} \rangle \cdot \langle 1_{\hat{i}}, 1_{\hat{z}} \mid + k[1, 0] \mid 0_{\hat{i}}, 0_{\hat{z}} \rangle \cdot \langle 0_{\hat{i}}, 1_{\hat{z}} \mid + k[1, 1] \mid 0_{\hat{i}}, 1_{\hat{z}} \rangle \cdot \langle 0_{\hat{i}}, 1_{\hat{z}} \mid + k[5, 0] \mid 0_{\hat{i}}, 0_{\hat{z}} \rangle \cdot \langle 2_{\hat{i}}, 1_{\hat{z}} \mid + k[5, 1] \mid 0_{\hat{i}}, 1_{\hat{z}} \rangle \cdot \langle 2_{\hat{i}}, 1_{\hat{z}} \mid$   
 $k[3, 2] \mid 1_{\hat{i}}, 0_{\hat{z}} \rangle \cdot \langle 1_{\hat{i}}, 1_{\hat{z}} \mid + k[3, 3] \mid 1_{\hat{i}}, 1_{\hat{z}} \rangle \cdot \langle 1_{\hat{i}}, 1_{\hat{z}} \mid + k[1, 2] \mid 1_{\hat{i}}, 0_{\hat{z}} \rangle \cdot \langle 0_{\hat{i}}, 1_{\hat{z}} \mid + k[1, 3] \mid 1_{\hat{i}}, 1_{\hat{z}} \rangle \cdot \langle 0_{\hat{i}}, 1_{\hat{z}} \mid + k[5, 2] \mid 1_{\hat{i}}, 0_{\hat{z}} \rangle \cdot \langle 2_{\hat{i}}, 1_{\hat{z}} \mid + k[5, 3] \mid 1_{\hat{i}}, 1_{\hat{z}} \rangle \cdot \langle 2_{\hat{i}}, 1_{\hat{z}} \mid$   
 $k[3, 4] \mid 2_{\hat{i}}, 0_{\hat{z}} \rangle \cdot \langle 1_{\hat{i}}, 1_{\hat{z}} \mid + k[3, 5] \mid 2_{\hat{i}}, 1_{\hat{z}} \rangle \cdot \langle 1_{\hat{i}}, 1_{\hat{z}} \mid + k[1, 4] \mid 2_{\hat{i}}, 0_{\hat{z}} \rangle \cdot \langle 0_{\hat{i}}, 1_{\hat{z}} \mid + k[1, 5] \mid 2_{\hat{i}}, 1_{\hat{z}} \rangle \cdot \langle 0_{\hat{i}}, 1_{\hat{z}} \mid + k[5, 4] \mid 2_{\hat{i}}, 0_{\hat{z}} \rangle \cdot \langle 2_{\hat{i}}, 1_{\hat{z}} \mid + k[5, 5] \mid 2_{\hat{i}}, 1_{\hat{z}} \rangle \cdot \langle 2_{\hat{i}}, 1_{\hat{z}} \mid$

# Bands corrected step by step



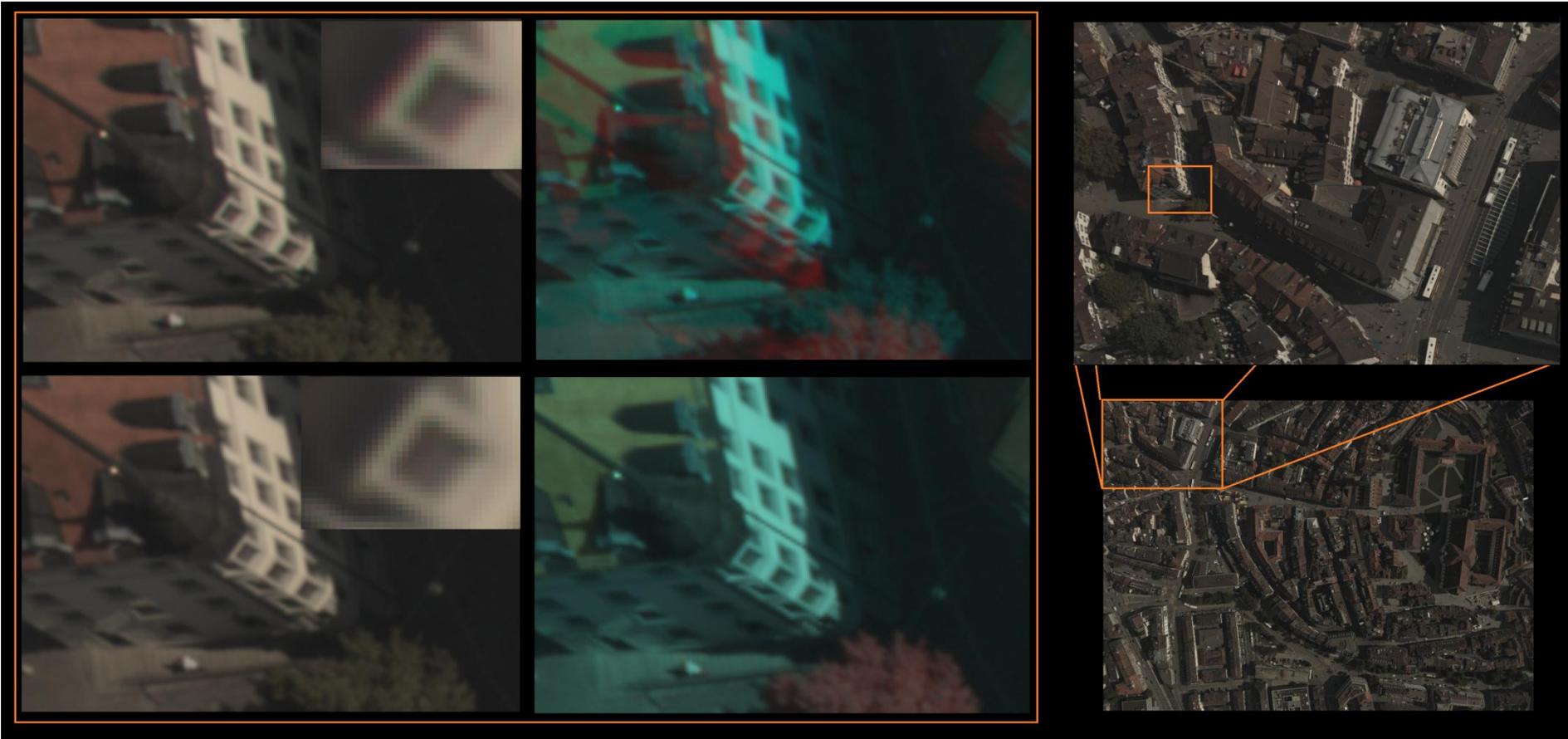


# Coregistration



Co-registration corrections

# Coregistration



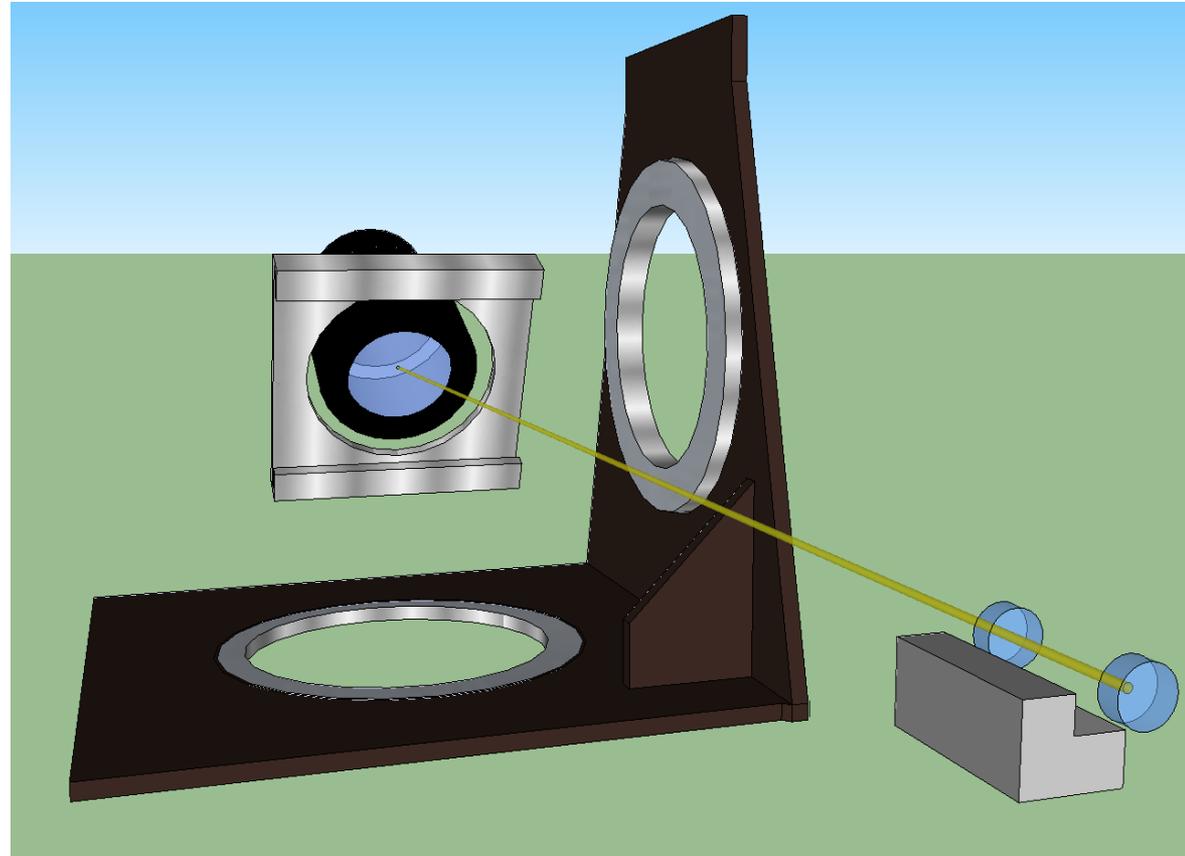


## Goniometry at Leica Geosystems

- T4 used for the RC20 calibration.
  - \* Design based on a high precision single axis
  - \* Not optimal for heavy lens systems
- Electronic Vertical Goniometer (EVG) used for the RC30 calibration
  - \* Also based on a High precision single axis but oriented vertically
  - \* Limited to measurements on the diagonal
  - \* Not usable for sensors with fixed focal plate (ADS40)
- Coded Vertical Goniometer (CVG) used for the ADS40 calibration
  - \* Dual axis EVG with fish bone oriented code bars
  - \* IR transmission performances and stability issues
  - \* Limited accuracy to 3 pixels

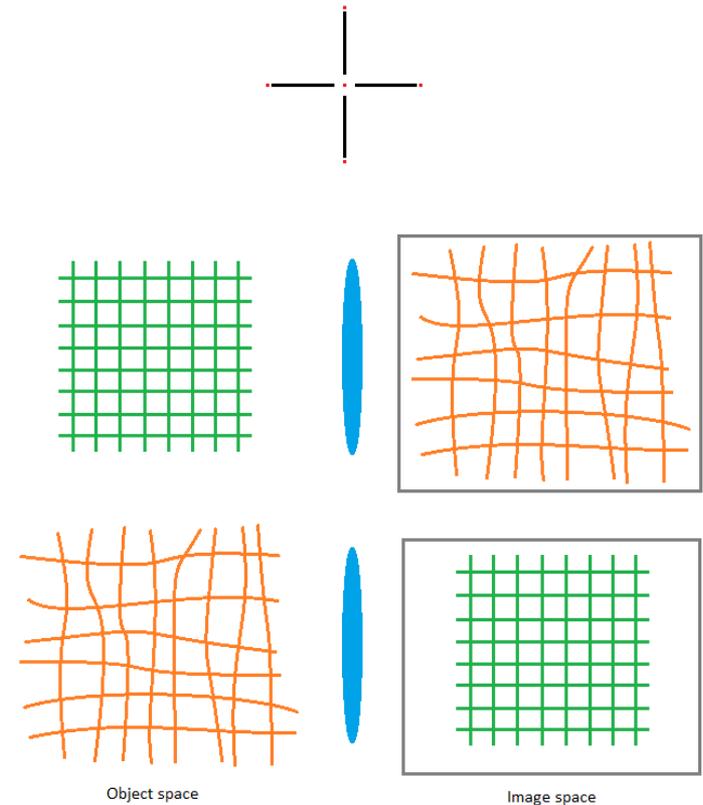
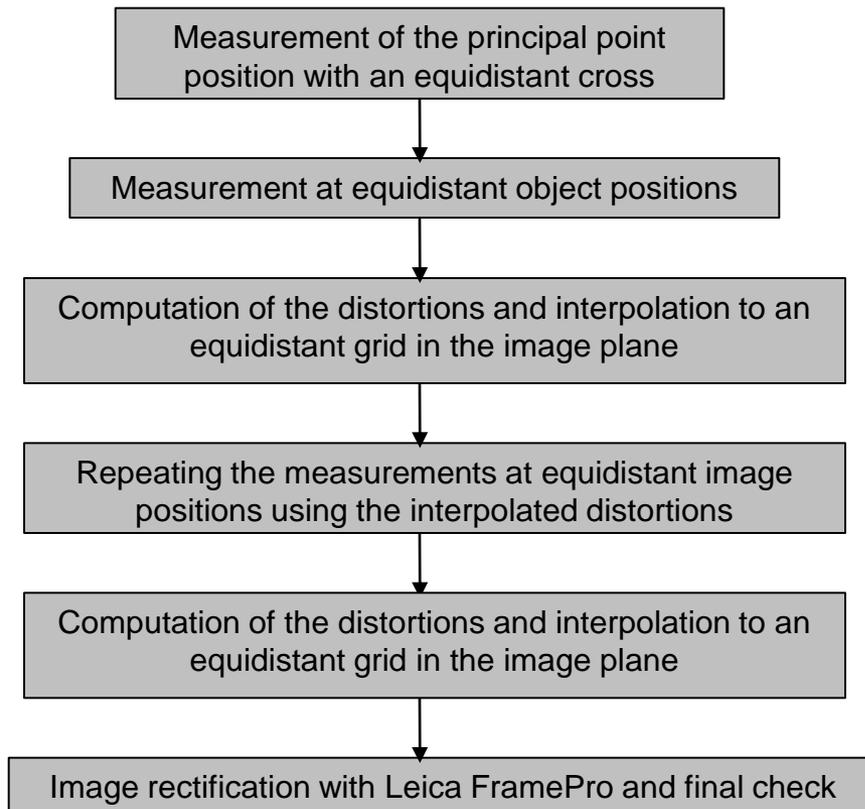
## RCD30 Goniometer design

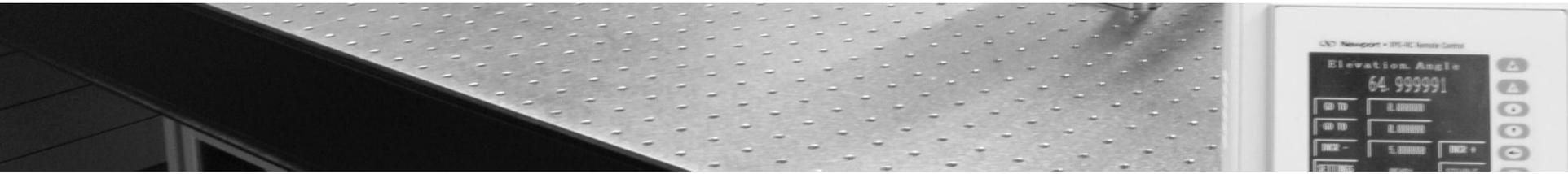
- Numerically controlled precision rotation stages (absolute error  $\pm 10''$  )
- Allow measurements in the direct and reverse positions
- Collimator used to project pinhole to infinity
- Autocollimation mode for infinity adjustment
- Mount for camera RCD30, RCD105
- Precise polygon mirror for goniometer calibration
- Temperature controlled room





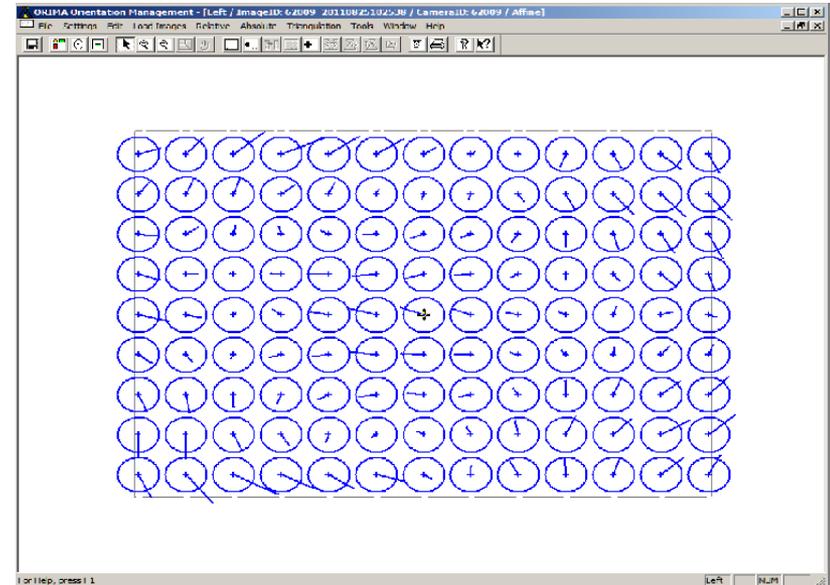
# RCD30 Goniometric calibration workflow





## Comparing the approaches

- Goniometry
  - \* independent from weather conditions
  - \* automatic procedure, reduced costs
- Flight
  - \* no need to ship a camera
  - \* IMU misalignment estimation
- Similar quality, comparisons still show effects in 1/3 pixel range.
- → Get better understanding of it.





Thank you!  
WRU

12.2.2012

The power to see



- when it has to be right

