

# Two-dimensional on-orbit MTF Analysis of Quickbird using Convex mirror Array

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## Introduction

- Objective**
  - One-dimensional (1-D) parametric techniques are commonly used to estimate system Point Spread Function (PSF)
  - Purpose was to estimate two-dimensional (2-D) PSF using a parametric method with convex mirrors as point sources.
  - Validation of results obtained from 2-D parametric method by comparing with results of 1-D non-parametric method.

- Point Spread Function (PSF)**
  - PSF is the Impulse response of the imaging system
  - For point source input, output of the system is two-dimensional PSF [Fig 1]
  - Convex mirror array were used as point sources for the Quickbird sensor

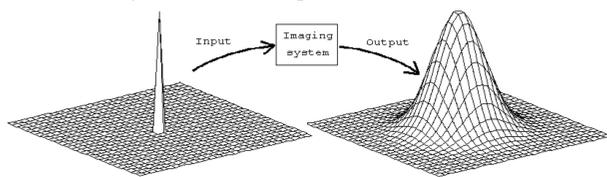


Figure 1. Two-dimensional PSF

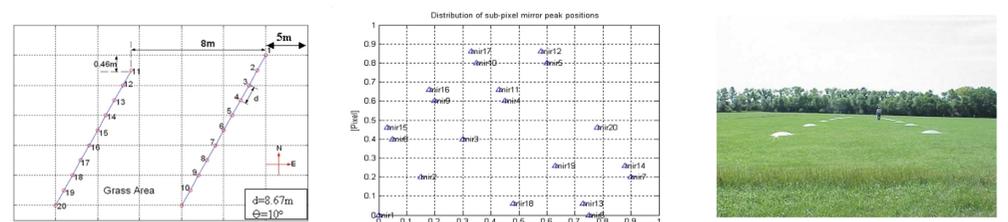
- Spatial Response components**
- Overall system PSF is represented by a combination of individual PSF's**
  - PSF due to characteristics of optical components
  - PSF due to motion of sensor over the scene
  - PSF due to characteristics of sensor electronics
  - PSF due to physical size and shape of detector elements
- Modulation Transfer function (MTF)**
  - MTF is an approach to determine the normalized frequency response of an imaging system.
  - MTF value at Nyquist frequency often used to specify spatial quality of an image



## Procedures

- Convex Mirror Dimension**
  - Focal length of convex mirror was calculated using the incident and at-sensor energy relation in [ Fig 2 ].
  - At-sensor radiance ( $E_s$ ) was calculated assuming DN value of 1638 (80% of Saturation level i.e.,  $2^{11} = 2048$ )
    - $DN = Gain * (At\ sensor\ radiance) + bias$
  - Attenuation constant  $k$  was calculated using IKONOS 2001 data **Figure 2. Mirror focal length**
  - Gain estimate was from current Quick-bird radiometric calibration
  - Sensor distance ( $d_{sat}$ ) was given as 450 km.
  - Incident sun radiance ( $E_i$ ) measured from Reagan sun photometer was  $1319\ W/m^2/sr$
  - Estimated focal length ( $f$ ) was 0.67 meters

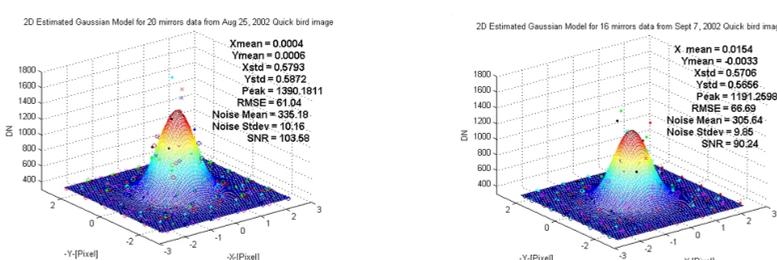
- Target development**
  - Angle and distance are critical to get a uniformly distributed sub-pixel sampled Point Spread Function (PSF) [Fig 3(b)]
  - Two columns of convex mirrors were placed on uniform grass background[Fig 3(c)]
  - Mirror array was inclined at an angle of  $10^\circ$  from North to East and were placed at a distance of 8.67m from each other to get desired uniform distribution.[Fig 3(a)]



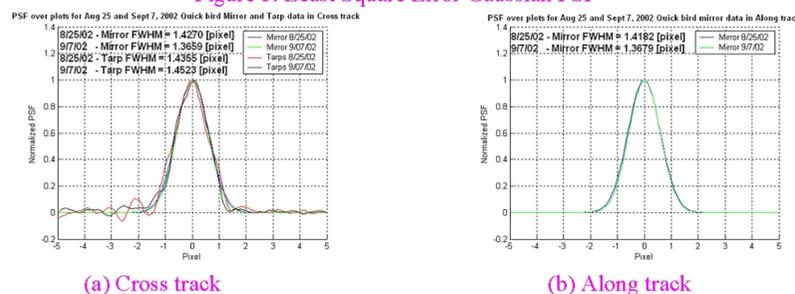
(a) Physical layout of mirror positions (b) Sampling distribution of Mirrors (c) Deployment  
Figure 3. Target development and deployment

- Simulation Steps**
  - Estimate peak location of each mirror by applying 2-D Gaussian model to individual mirror responses [Fig 4(a)]
  - Align to a common reference grid [Fig 4(b)]
  - Apply 2-D Gaussian model on the aligned data set to estimate the PSF of imaging system [Fig 4(c)]
  - Estimate Full Width of Half Maximum (FWHM) measurements from one-dimensional profiles of PSF in cross and along track directions [Fig 4(d)].
  - Obtain normalized MTF values at Nyquist frequency in cross and along track directions by applying Fourier transform on 1-D PSF profiles [Fig 4(e)]

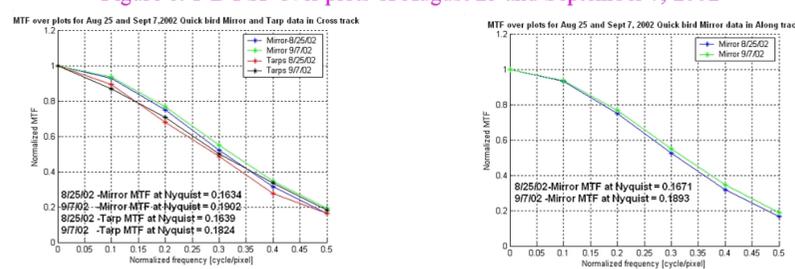
## Results: Applied on Quickbird 2002 images



(a) August 25, 2002 (b) September 7, 2002  
Figure 5. Least Square Error Gaussian PSF



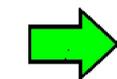
(a) Cross track (b) Along track  
Figure 6. 1-D PSF over plots of August 25 and September 7, 2002



(a) Cross track (b) Along track  
Figure 7. 1-D MTF over plots of August 25 and September 7, 2002

- Comparison of FWHM and MTF values obtained using parametric, two-dimensional Gaussian model and non-parametric methods**

Panband	PSF				MTF			
	08/25/02		09/07/02		08/25/02		09/07/02	
Quick-bird	Along track	Cross track						
2002 Targets								
Mirrors	1.4187	1.427	1.3679	1.3659	0.1671	0.1634	0.1893	0.1902
Taps	n/a	1.4355	n/a	1.4523	n/a	0.1639	n/a	0.1824



## Conclusions

- MTF values (normalized) at Nyquist frequency ranges from 0.16 to 0.19 in cross track and 0.17 to 0.19 in along track direction.
- MTF and FWHM measurements obtained from the two-dimensional parametric method were validated by results obtained previously from one-dimensional parametric method.
- Physical layout of point sources (mirrors) is extremely important for PSF measurement.
- Quick-bird imagery met the NASA SDP specification.

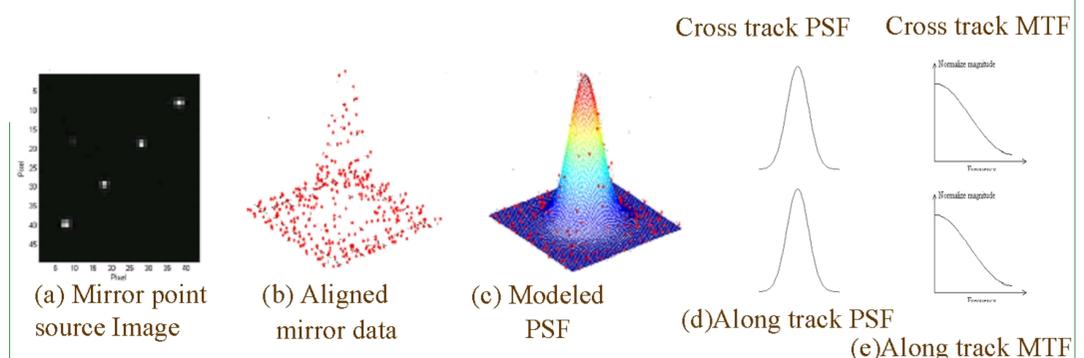


Figure 4. Two-dimensional MTF estimation